

Opportunities & challenges in graph-based learning for power system application

Delft AI Energy Lab

Mission & objective

- combine groundbreaking ML with the reliable theory of the physical energy system
- make energy systems sustainable, reliable, effective

Education

- EE4C12 ML for Electrical Engineering
- SET 3125 Machine Learning Workflows for Digital Energy Systems
- SC42150 Statistical Signal Processing
- SC42110 Dynamic Programming and Stochastic Control
- MOOC Digitalization of Intelligent and Integrated Energy Systems
- Crash course of “Data-science”

Research

- Supervised learning for real-time grid assessment
- Distributed learning for power system congestion management
- Data-driven grid models for electricity load and weather forecasts
- Characterizing healthy/normal trajectories of complex dynamical systems using dictionary learning
- From fast Fourier transform to fast reinforcement learning

Key innovations

- AI-based algorithms for grid operation
- Real-time security assessment and anomaly detection
- Real-time learning algorithms for control and security of complex dynamical systems

Team



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Acknowledgements



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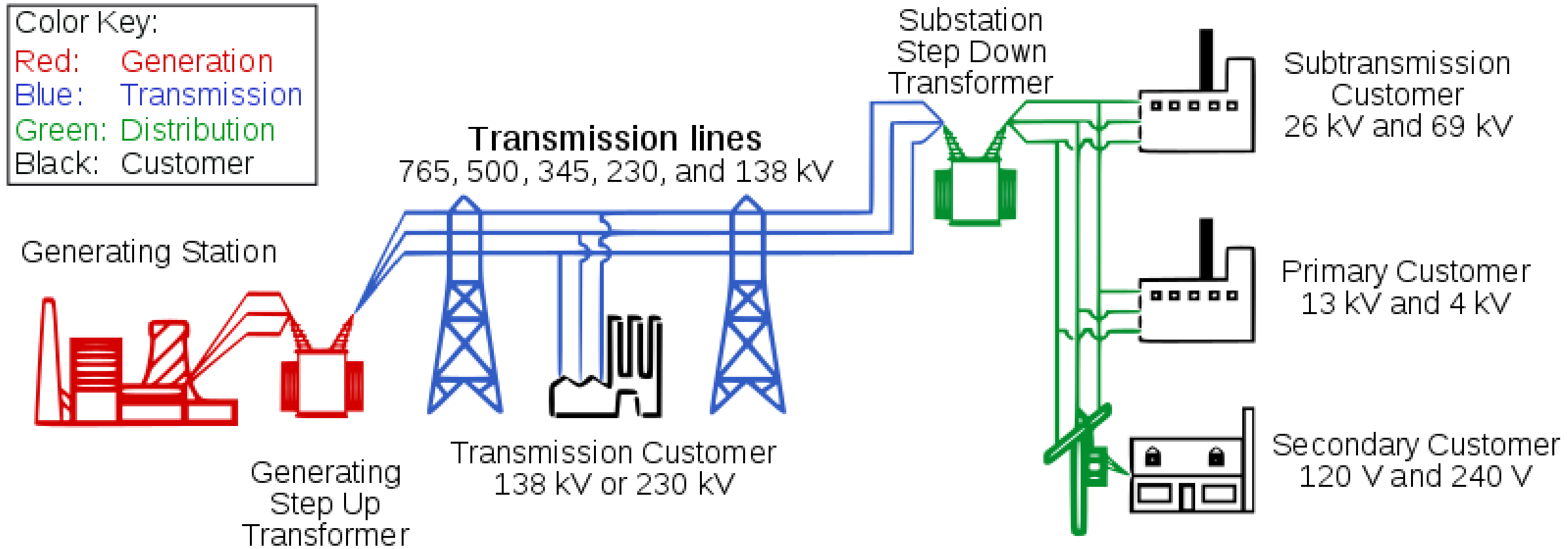


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Betuel Mamudi

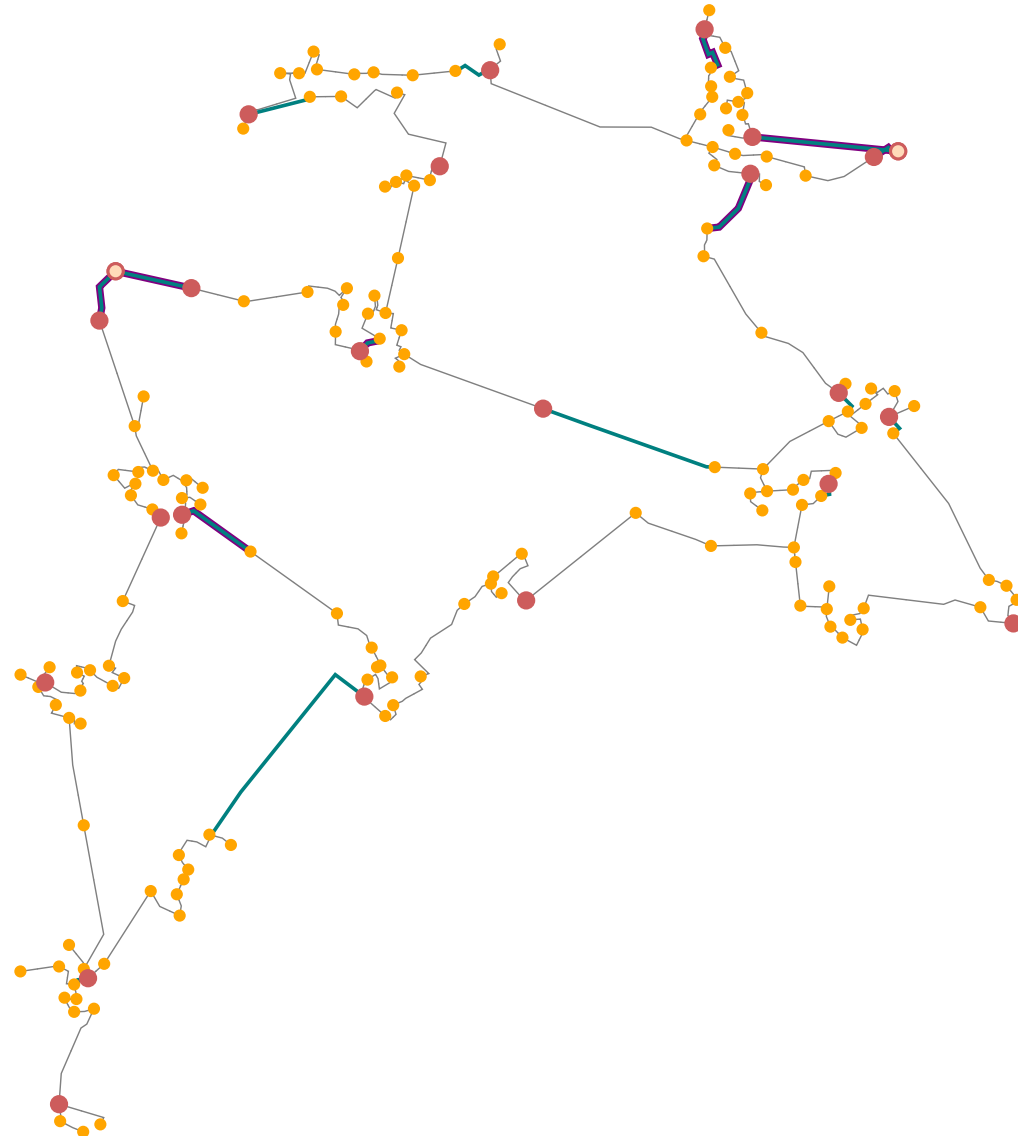
Power systems





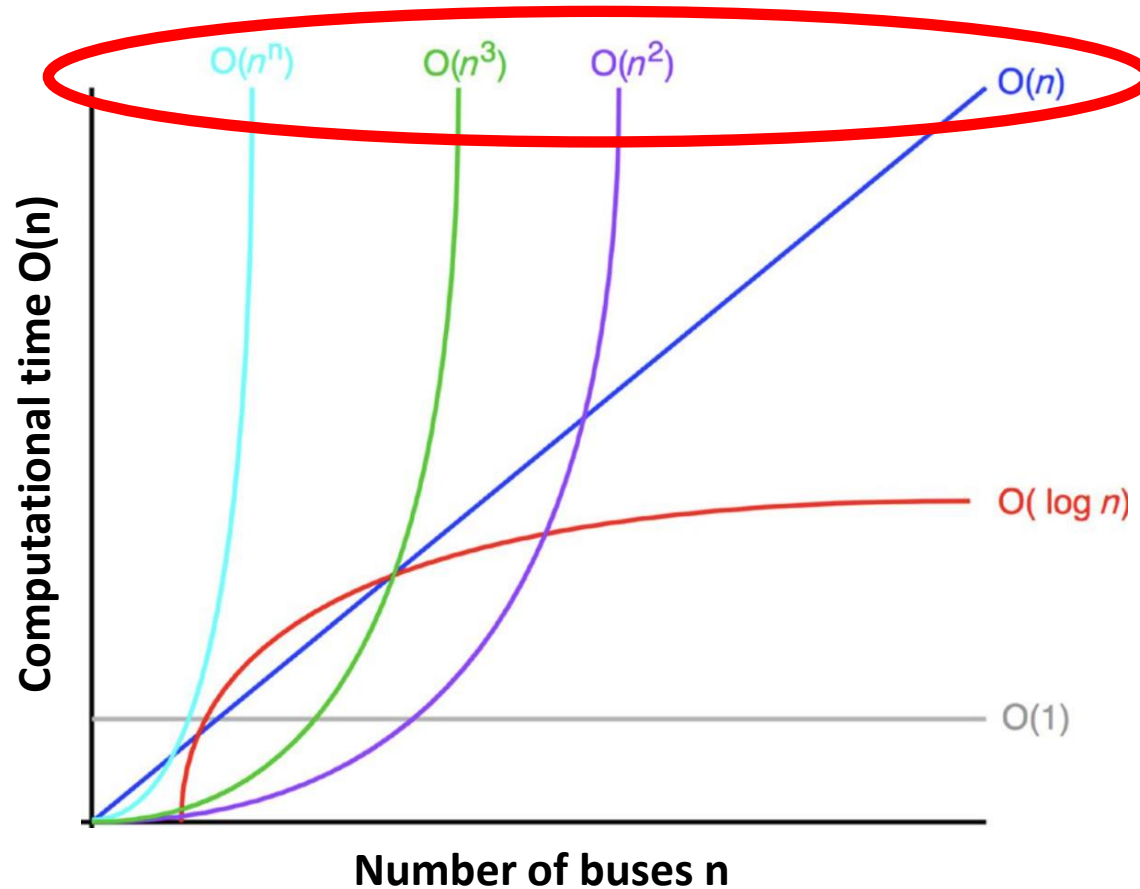
Distribution system (MV)

- Trafo
- Lines
- MV/LV buses
- HV buses
- Power flow measurement
- Voltage measurements
- Focus bus



Scaling power system analysis to very large grids

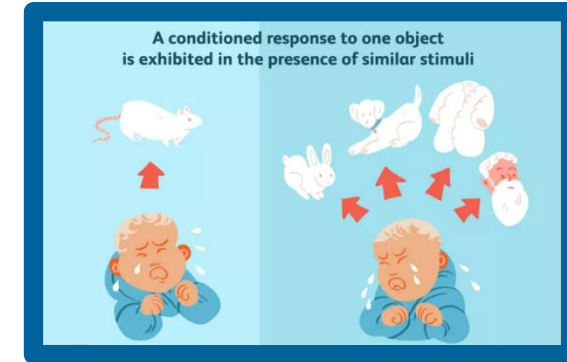
Example: reliability assessment



What are barriers applying AI?

1. Generalising to out-of-distribution data

- Different energy scenarios in the future
- Historical observations are not suitable
- Energy systems will be ever-evolving

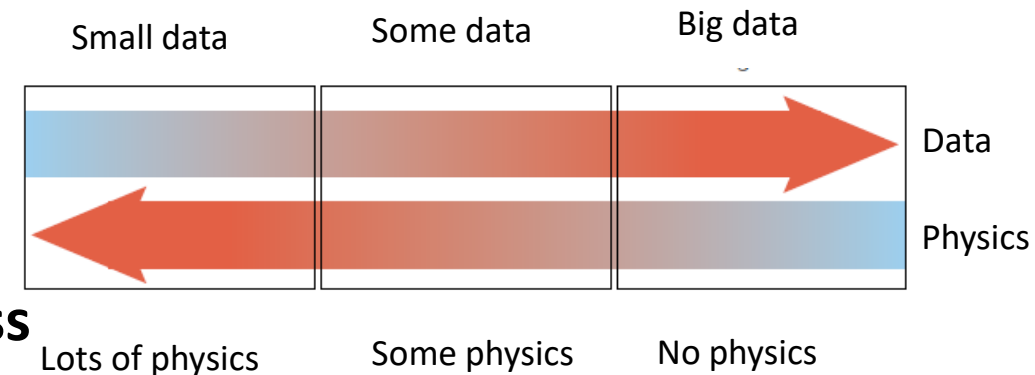


2. Large training data is needed

- Power systems are extremely large systems
- Training an AI for such large systems requires a lot of data

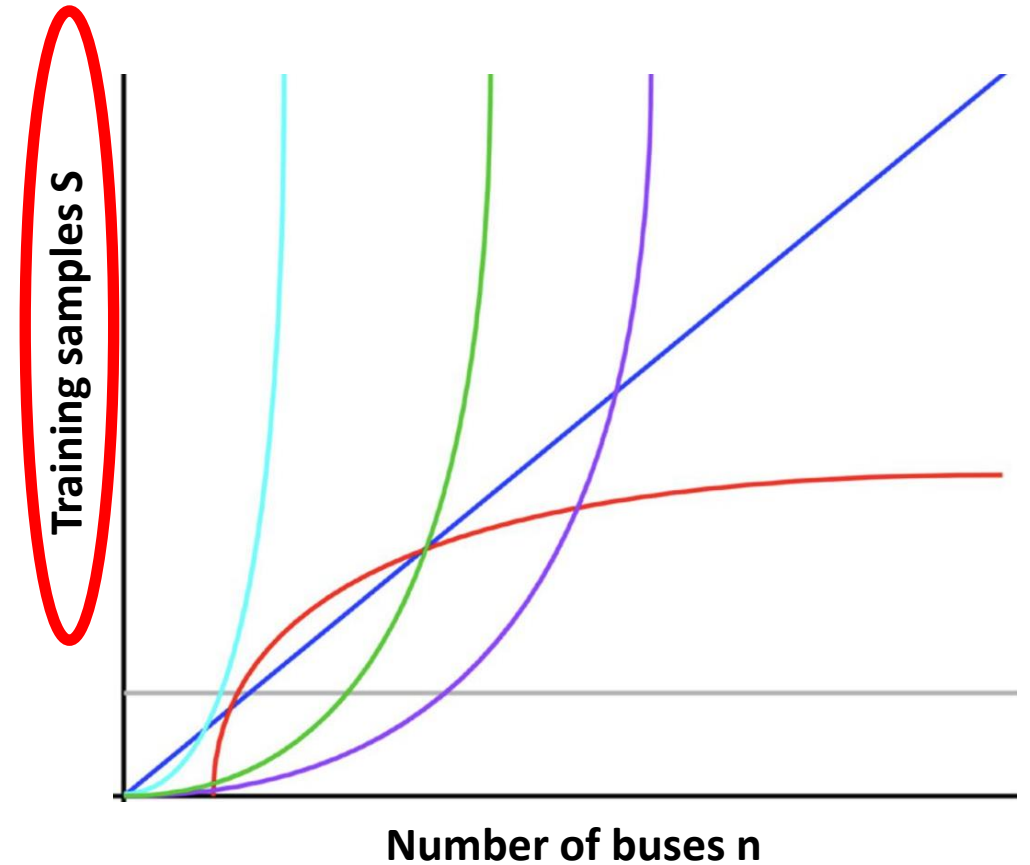
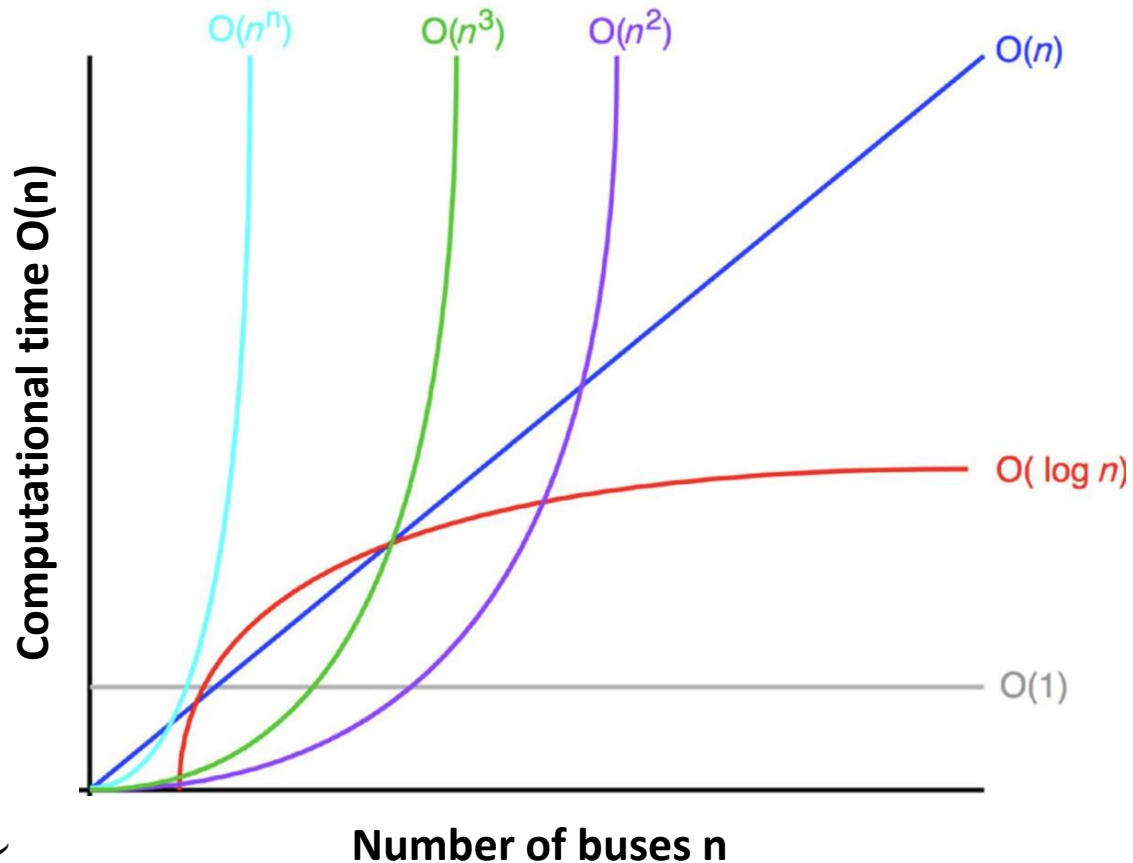
3. AI does not provide explanations or robustness

- Energy systems are critical and sensitive infrastructures



ML-driven 'proxies' for power system analysis

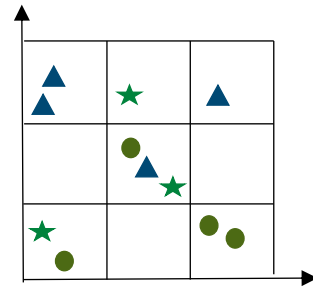
Challenge: scaling to system size



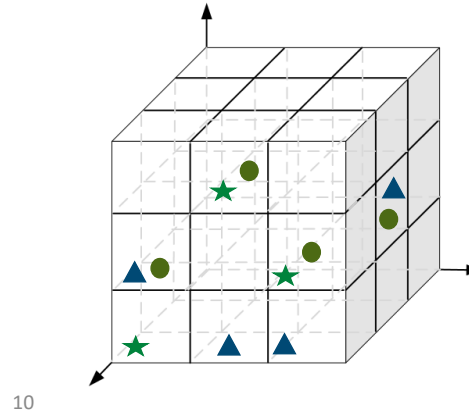
Curse of dimensionality



1d: 3 regions



2d: 3^2 regions



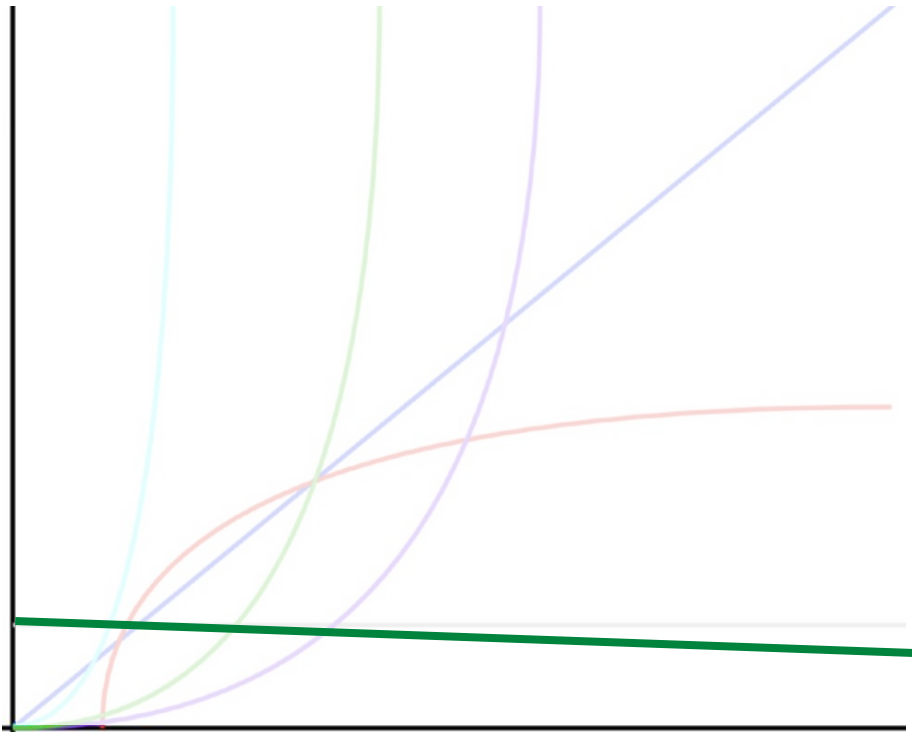
3d: 3^3 regions



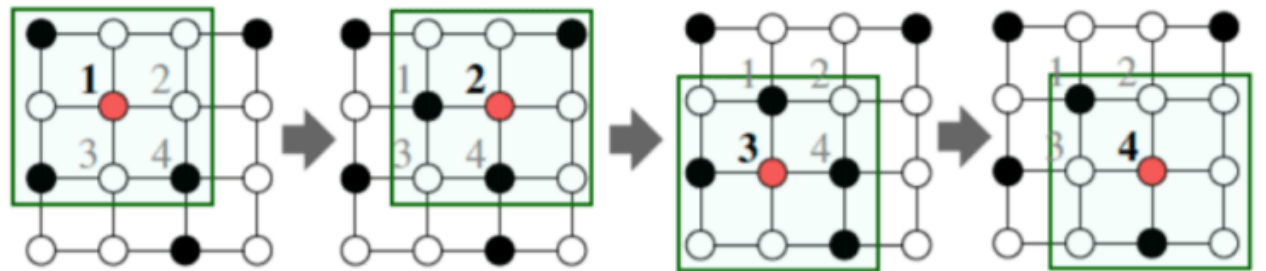
As dimensionality grows: fewer samples per region.

Learning without labels and inducing bias

- Self-supervised learning
- Physics-informed ML
- Weakly-supervised learning



Utopia?



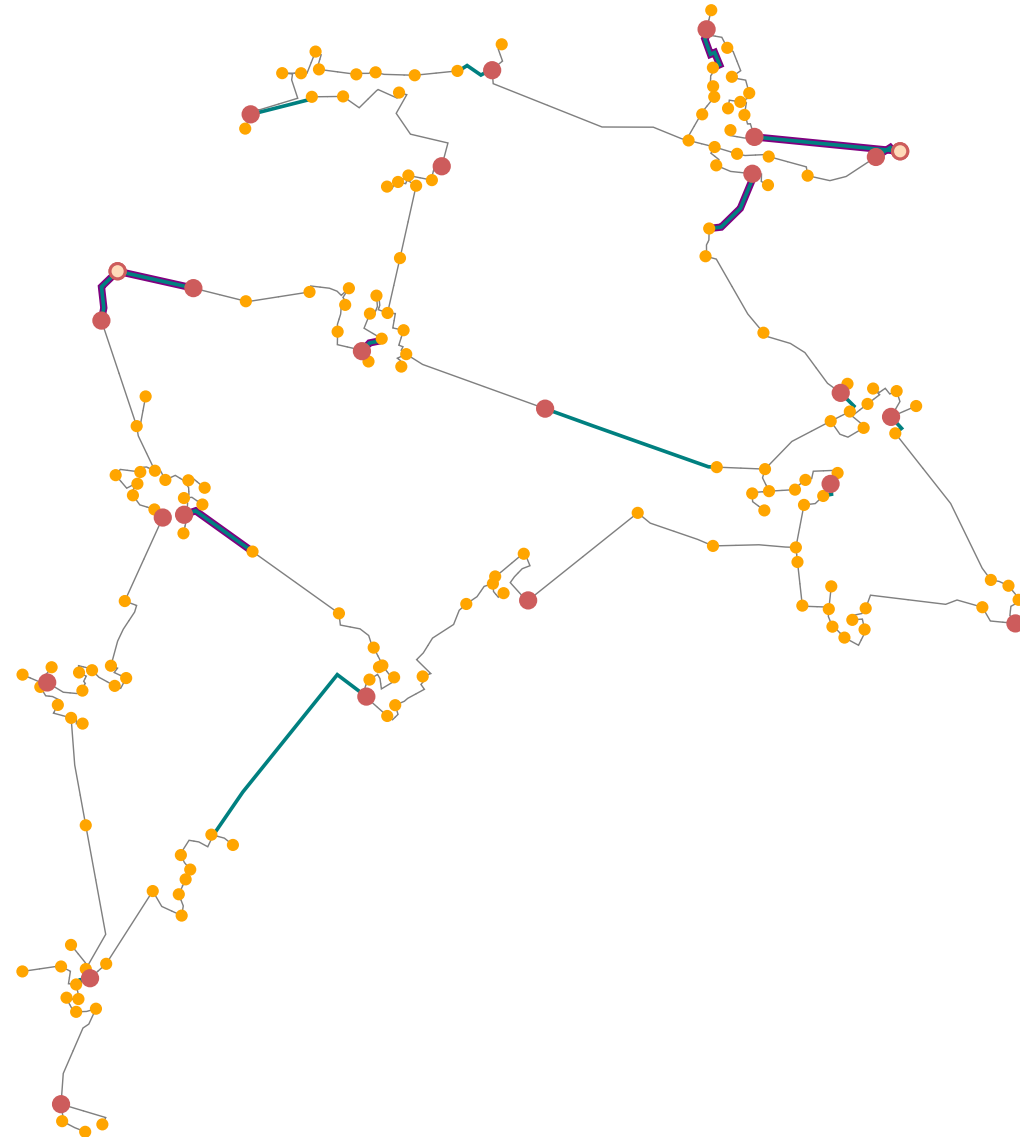
Graph neural networks
learn from the neighbours

Distribution system state estimation

- Measurements $z \in \mathbb{R}^m$ with noise $\varepsilon \in \mathbb{R}^m$
- System state $x \in \mathbb{R}^{2n}$
- State estimation $f(z) \rightarrow x$
- Challenge: partial observable, scarce measurements $m \ll n$

Distribution system (MV)

- Trafo
- Lines
- MV/LV buses
- HV buses
- Power flow measurement
- Voltage measurements



Model of the power flow

$$x = [V, \varphi]$$

$$z = h(x) + \varepsilon$$

$h(x) =$

$$V_i = V_i$$

$$\varphi_i = \varphi_i$$

$$P_{ij \rightarrow} = -V_i V_j [\Re(Y_{ij}) \cos \Delta\varphi_{ij} + \Im(Y_{ij}) \sin \Delta\varphi_{ij}] + V_i^2 \left[\Re(Y_{ij}) + \frac{\Re(Y_{sij})}{2} \right]$$

$$P_{ij \leftarrow} = V_i V_j [-\Re(Y_{ij}) \cos \Delta\varphi_{ij} + \Im(Y_{ij}) \sin \Delta\varphi_{ij}] + V_j^2 \left[\Re(Y_{ij}) + \frac{\Re(Y_{sij})}{2} \right]$$

$$Q_{ij \rightarrow} = V_i V_j [-\Re(Y_{ij}) \sin \Delta\varphi_{ij} + \Im(Y_{ij}) \cos \Delta\varphi_{ij}] - V_i^2 \left[\Im(Y_{ij}) + \frac{\Im(Y_{sij})}{2} \right]$$

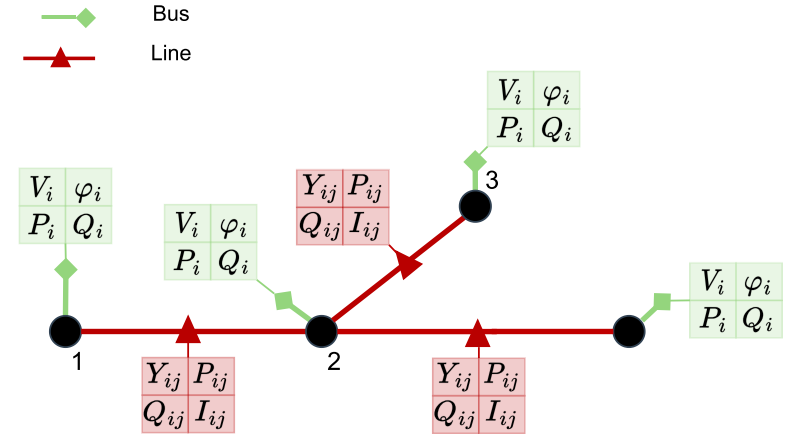
$$Q_{ij \leftarrow} = V_i V_j [\Re(Y_{ij}) \sin \Delta\varphi_{ij} + \Im(Y_{ij}) \cos \Delta\varphi_{ij}] - V_j^2 \left[\Im(Y_{ij}) + \frac{\Im(Y_{sij})}{2} \right]$$

$$I_{ij \rightarrow} = - \frac{P_{ij \rightarrow} - jQ_{ij \rightarrow}}{\sqrt{3}V_i e^{-j\varphi_i}}$$

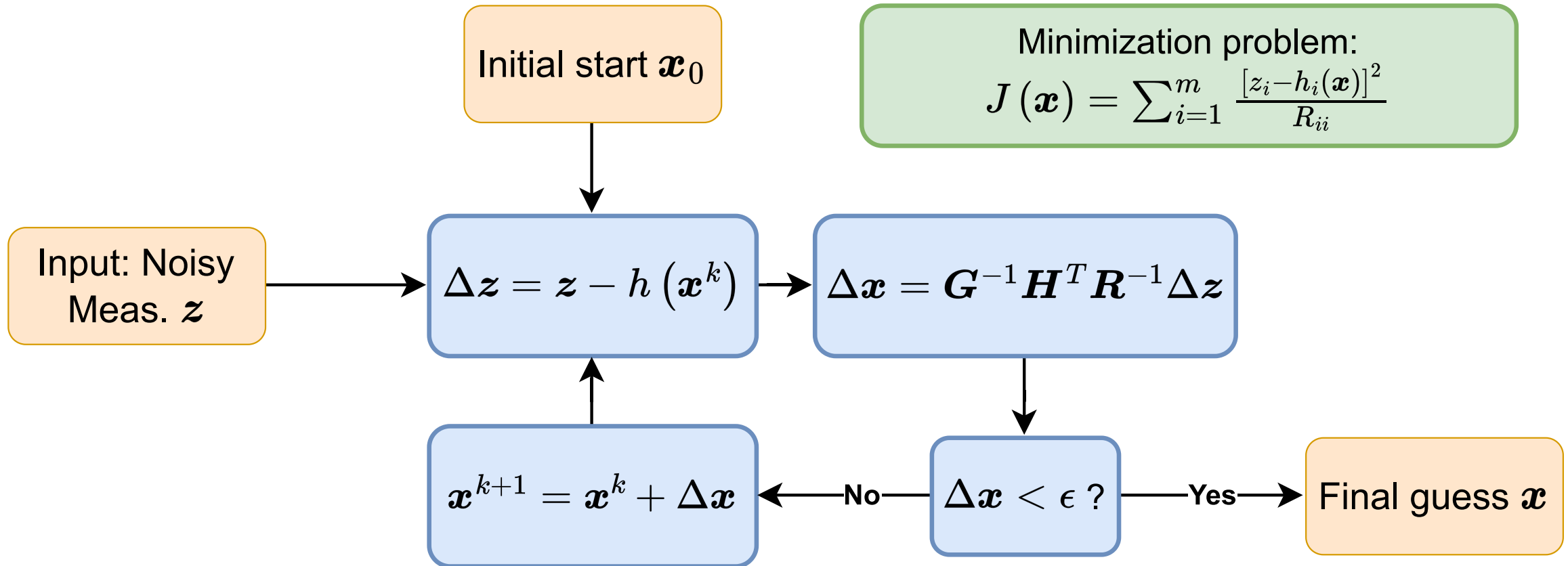
$$I_{ij \leftarrow} = - \frac{P_{ij \leftarrow} - jQ_{ij \leftarrow}}{\sqrt{3}V_j e^{-j\varphi_j}}$$

$$P_i = - \sum_{j \in N_x(i)} P_{ij \leftarrow} + P_{ij \rightarrow}$$

$$Q_i = - \sum_{j \in N_x(i)} Q_{ij \leftarrow} + Q_{ij \rightarrow}$$



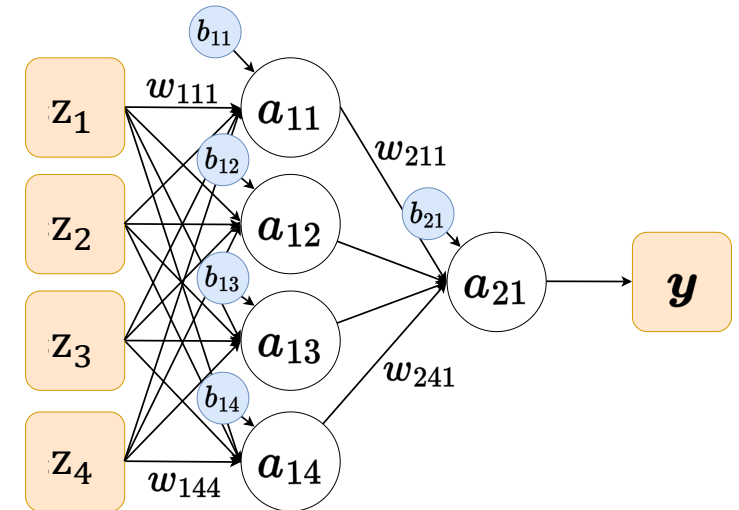
Weighted least squares method



Statistical learning

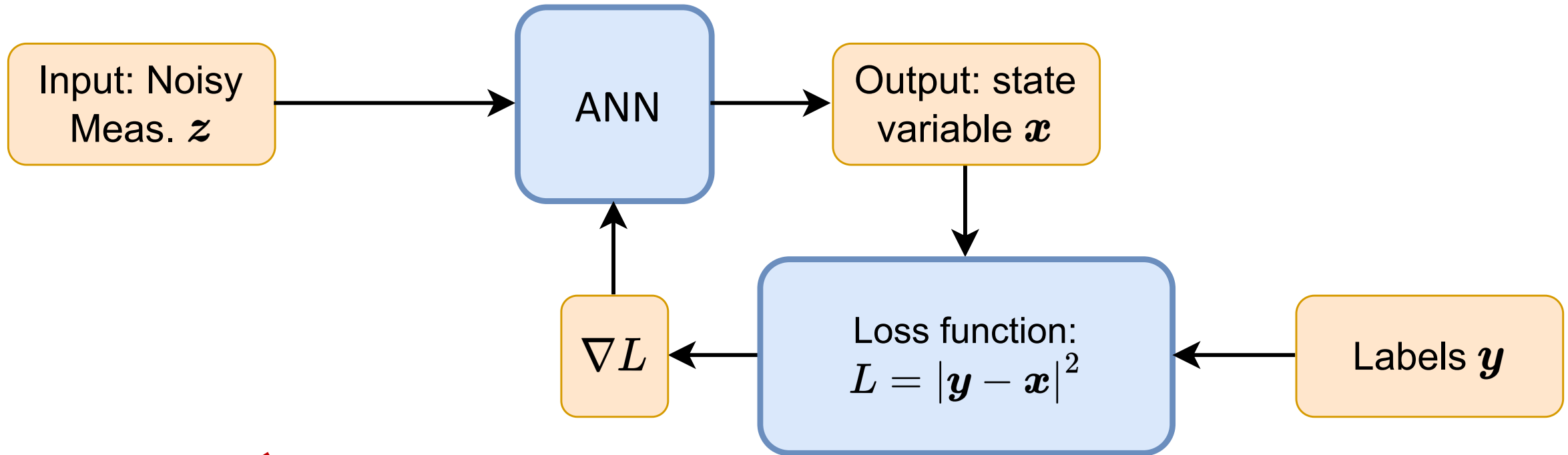
- Training set $S = \{(z_1, y_1), (z_2, y_2) \dots (z_t, y_t)\}$ with t samples
- Inference problem is to find a function $f: Z \rightarrow Y$ such that $f(z) \sim y$
- Common loss function $L(f(z), y)$ for regression is the square loss

Artificial Neural Network (ANN)



$$f_{\theta}: Z \rightarrow Y$$

Supervised learning for state estimation



⚡ Labels are not known

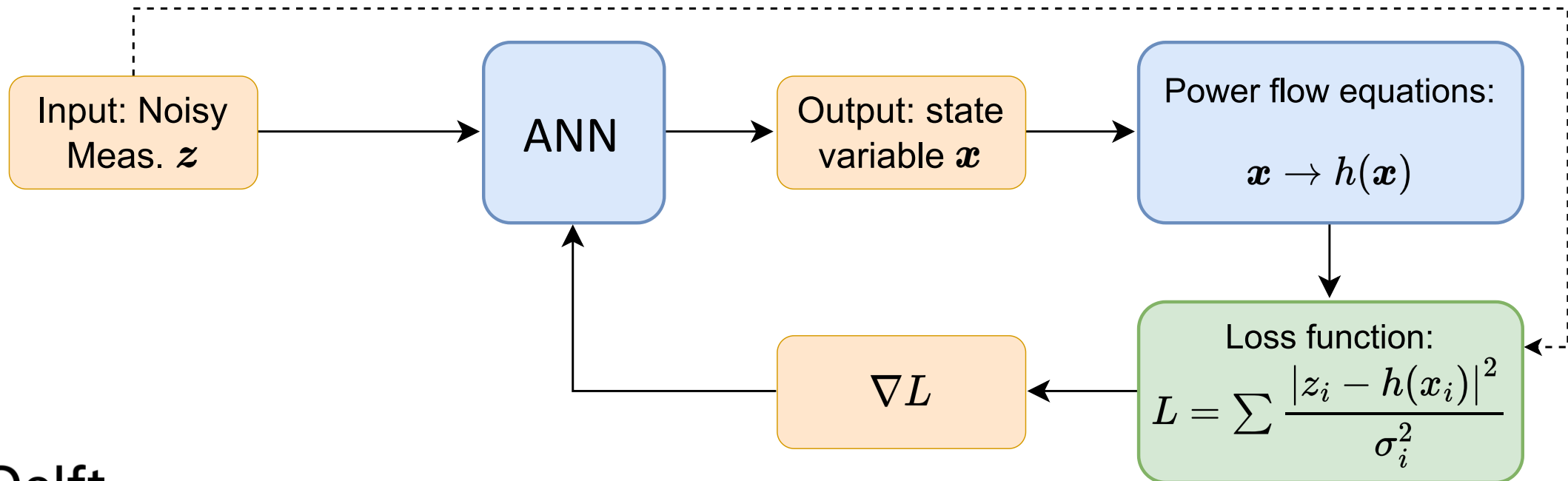
⚡ Newton's method generates label with "errors" $\hat{y} = y + \gamma^N$

Weakly-supervised learning

- Inaccurate input and **output**
- Learn with inaccurate labels $S = \{(z_1, \hat{y}_1), (z_2, \hat{y}_2) \dots (z_t, \hat{y}_t)\}$
- Design a loss function $L(f(z), \hat{y})$
- Objective: learning $f: Z \rightarrow Y$ such that $f(z) \sim y$

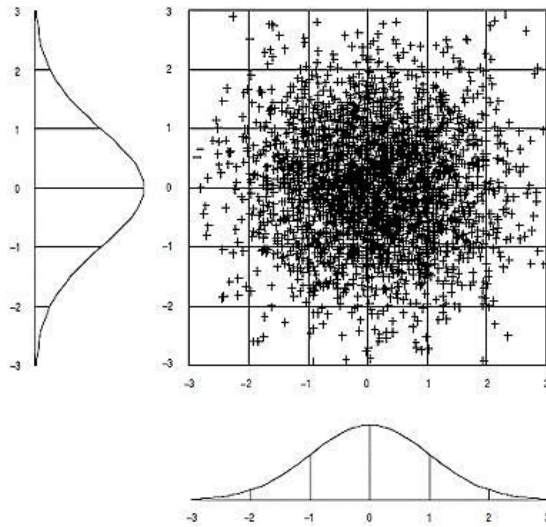
Weakly-supervised learning for state estimation

- ANN $f(z) \rightarrow x$
- Measurement function using power flow equations $h(x) \rightarrow \hat{z}$



Respect the structure of the domain

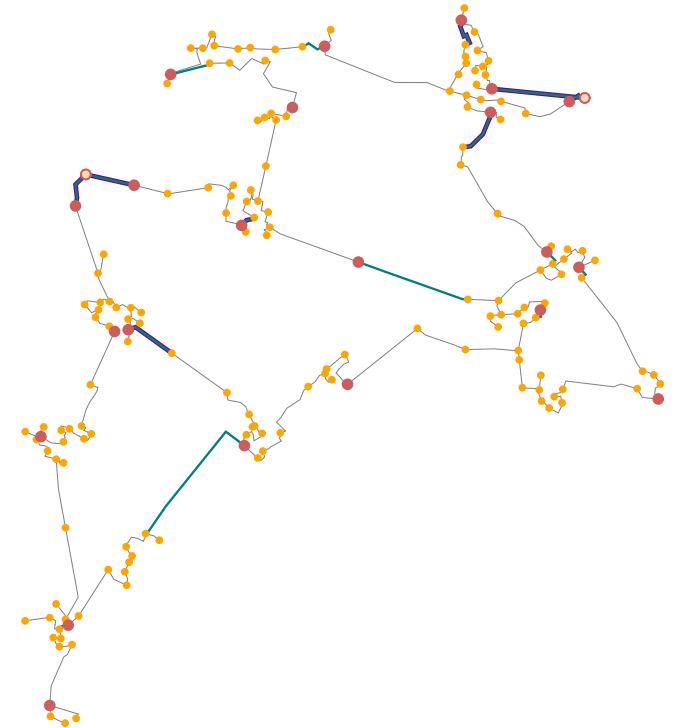
Noisy measurements



Power flow equations

$$h(x) = \begin{cases} V_i = V_i \\ \varphi_i = \varphi_i \\ P_{ij \rightarrow} = -V_i V_j [\Re(Y_{ij}) \cos \Delta \varphi_{ij} + \Im(Y_{ij}) \sin \Delta \varphi_{ij}] + V_i^2 \left[\Re(Y_{ij}) + \frac{\Re(Y_{sij})}{2} \right] \\ P_{ij \leftarrow} = V_i V_j [-\Re(Y_{ij}) \cos \Delta \varphi_{ij} + \Im(Y_{ij}) \sin \Delta \varphi_{ij}] + V_j^2 \left[\Re(Y_{ij}) + \frac{\Re(Y_{sij})}{2} \right] \\ Q_{ij \rightarrow} = V_i V_j [-\Re(Y_{ij}) \sin \Delta \varphi_{ij} + \Im(Y_{ij}) \cos \Delta \varphi_{ij}] - V_i^2 \left[\Im(Y_{ij}) + \frac{\Im(Y_{sij})}{2} \right] \\ Q_{ij \leftarrow} = V_i V_j [\Re(Y_{ij}) \sin \Delta \varphi_{ij} + \Im(Y_{ij}) \cos \Delta \varphi_{ij}] - V_j^2 \left[\Im(Y_{ij}) + \frac{\Im(Y_{sij})}{2} \right] \\ I_{ij \rightarrow} = -\frac{P_{ij \rightarrow} - jQ_{ij \rightarrow}}{\sqrt{3}V_i e^{-j\varphi_i}} \\ I_{ij \leftarrow} = -\frac{P_{ij \leftarrow} - jQ_{ij \leftarrow}}{\sqrt{3}V_j e^{-j\varphi_j}} \\ P_i = -\sum_{j \in N_x(i)} P_{ij \leftarrow} + P_{ij \rightarrow} \\ Q_i = -\sum_{j \in N_x(i)} Q_{ij \leftarrow} + Q_{ij \rightarrow} \end{cases}$$

Topology

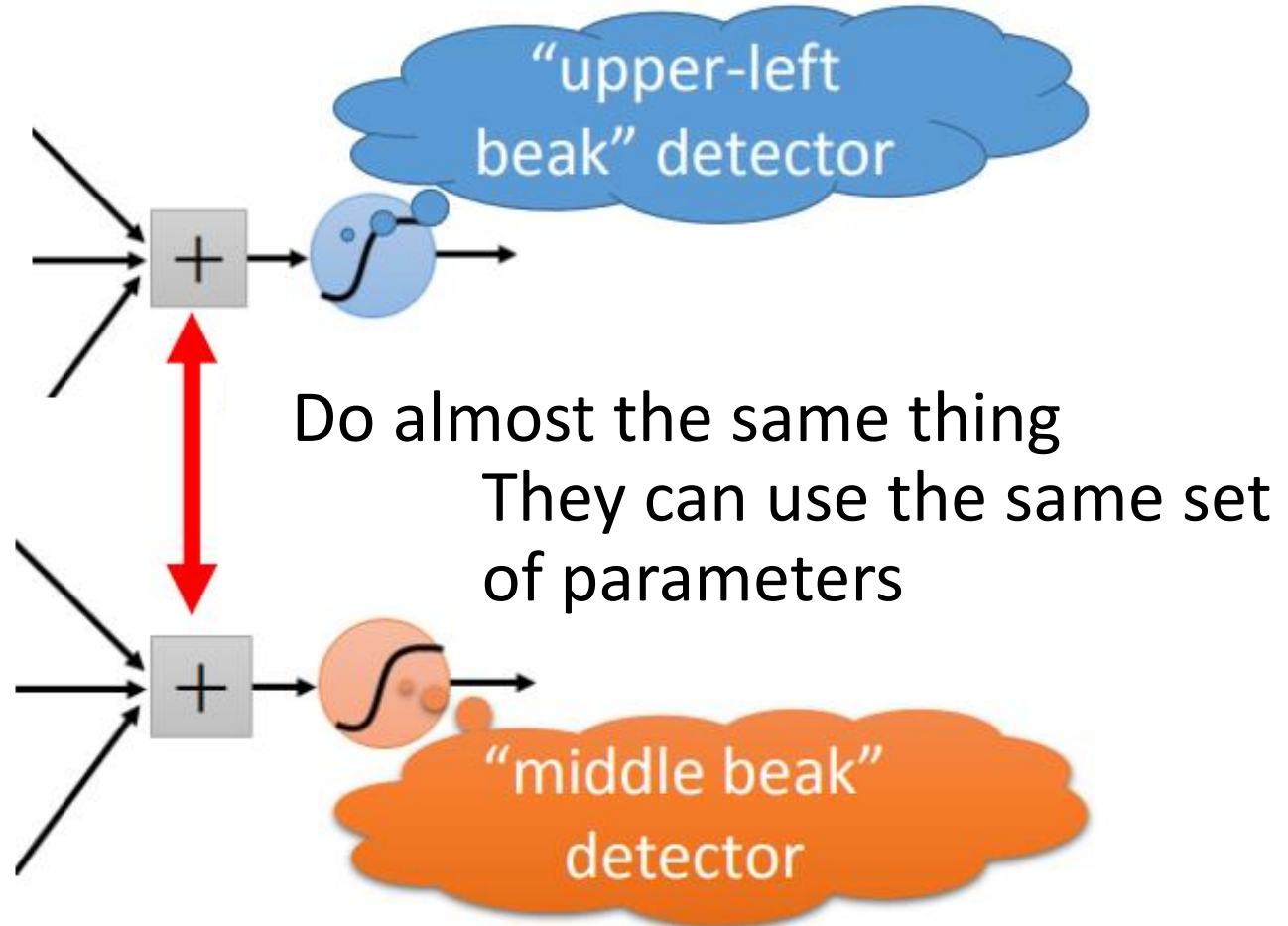
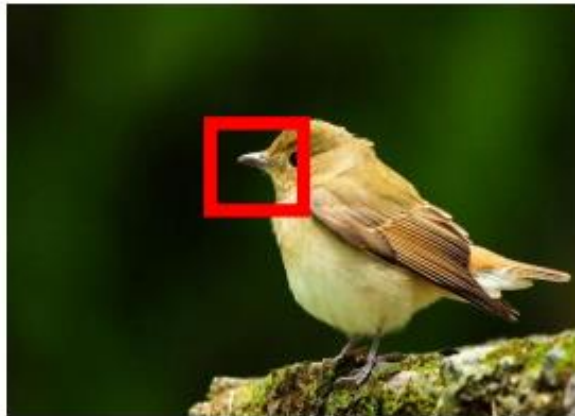


AI successes in the domain ‘images’

Property 1: Some patterns are much smaller than the whole image. A neuron does not have to see the whole image to discover the pattern.



Property 2: The same patterns appear in different regions. (translated invariance)



CNN— Convolution layer

Stride=1

1	0	0	0	0	1
0	1	0	0	1	0
0	0	1	1	0	0
0	0	0	0	1	0
1	1	1	0	1	0
0	0	0	0	1	0

6×6 image

Those are the network parameters to be learned

1	-1	-1
-1	1	-1
-1	-1	1

Filter 1
Matrix

-1	1	-1
-1	1	-1
-1	1	-1

Filter 2
Matrix



3	-1	-3	-1
-2	1	-1	-3
-2	-4	0	1
-1	0	-2	-1

Property 1

Each filter detects a small pattern (3 x 3)

CNN— Convolution layer

Stride=1

0	1	0	0	0	1
0	1	0	0	1	0
0	0	0	1	0	0
0	0	0	1	0	0
1	1	1	0	1	0
0	0	0	0	0	1

6×6 image

1	-1	-1
-1	1	-1
-1	-1	1

Filter 1
Matrix



0	1	-2	-1
-1	1	-1	-3
-1	-4	0	-1
-1	-1	-3	3

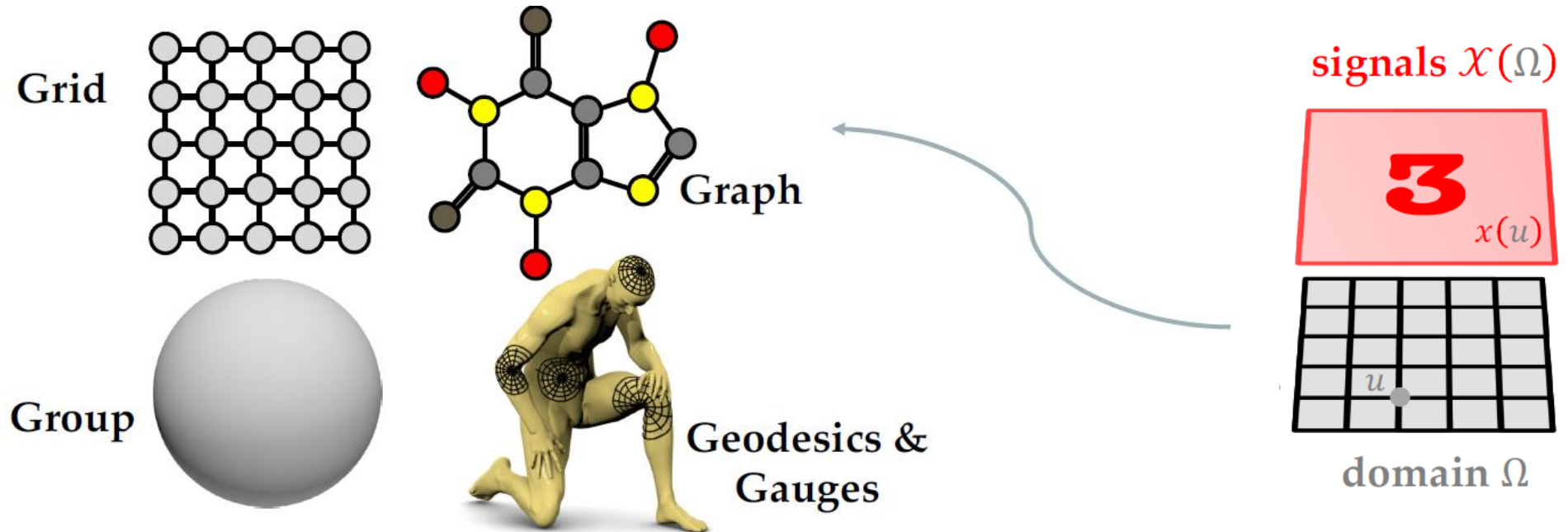
Property 2

The same patterns that appear in different regions can be detected.

**Not much image-like data in power system
operation and planning...**

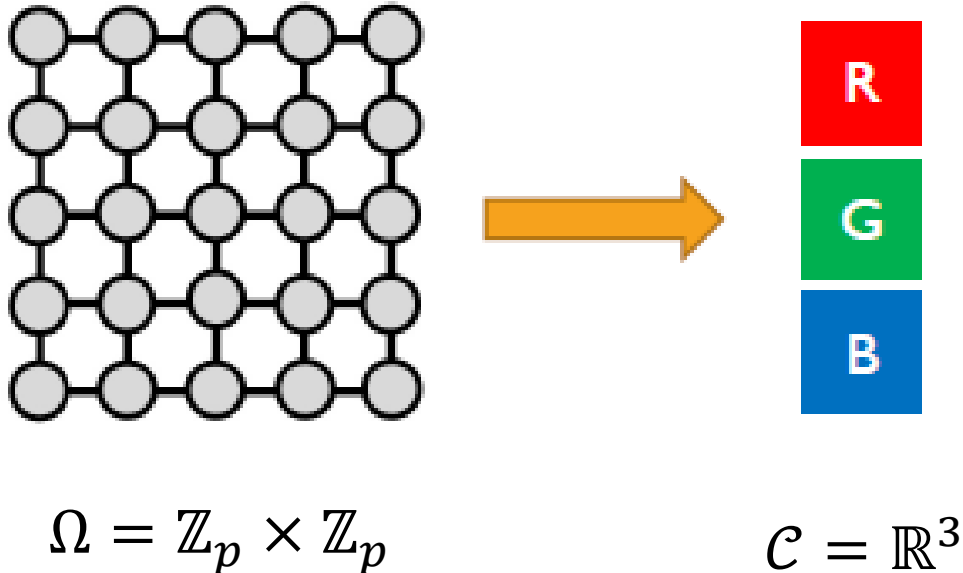
Geometric deep learning

- Data are signals x on geometric domains Ω
- A signal x on Ω is a function $\chi(\Omega, \mathcal{C}) = \{x: \Omega \rightarrow \mathcal{C}\}$

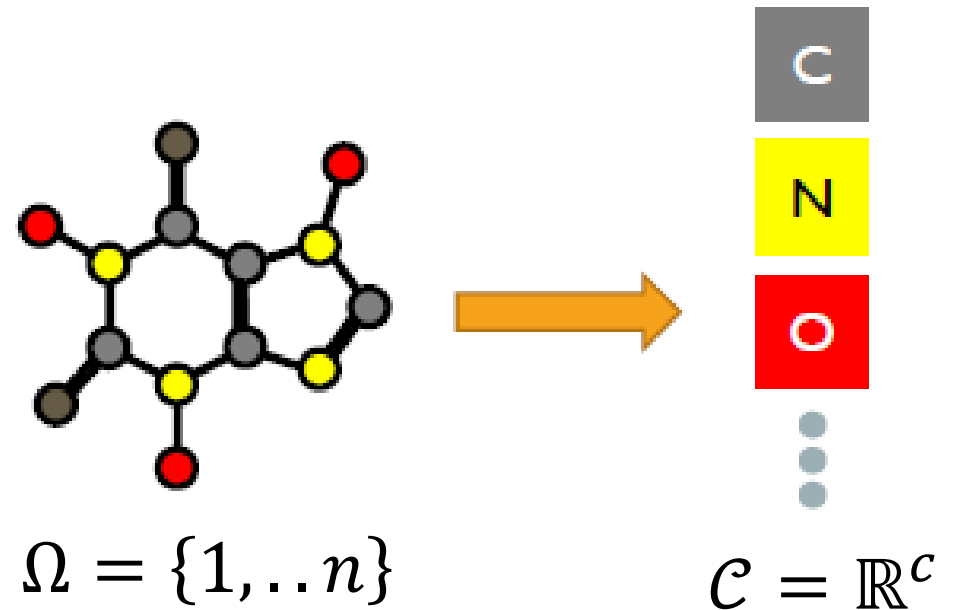


Graph Neural Networks (GNNs)

Example: $p \times p$ RGB image



Example: molecular graph



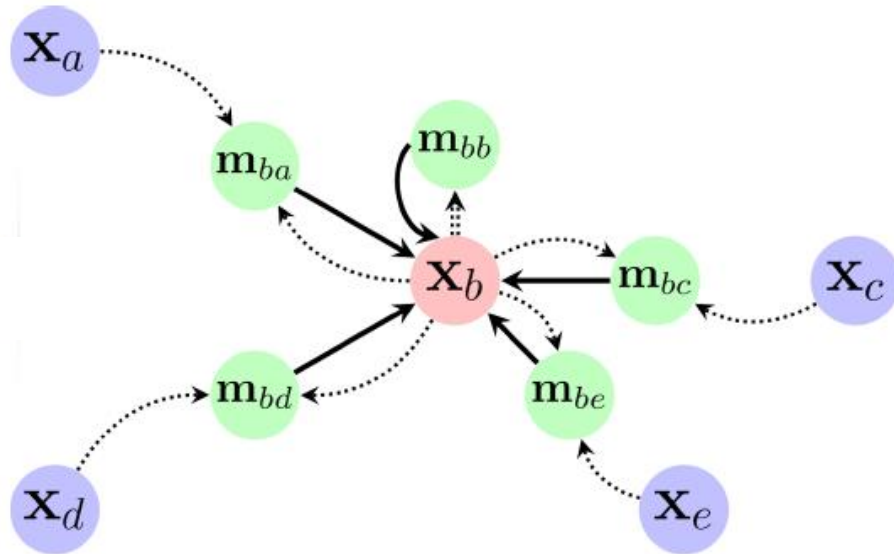
Locality on graphs: Neighbourhoods

- Consider graph $G = (V, E)$ where $E \subseteq V \times V$
- Adjacency matrix A with

$$a_{ij} = \begin{cases} 1, & (i, j) \in E \\ 0, & (i, j) \notin E \end{cases}$$

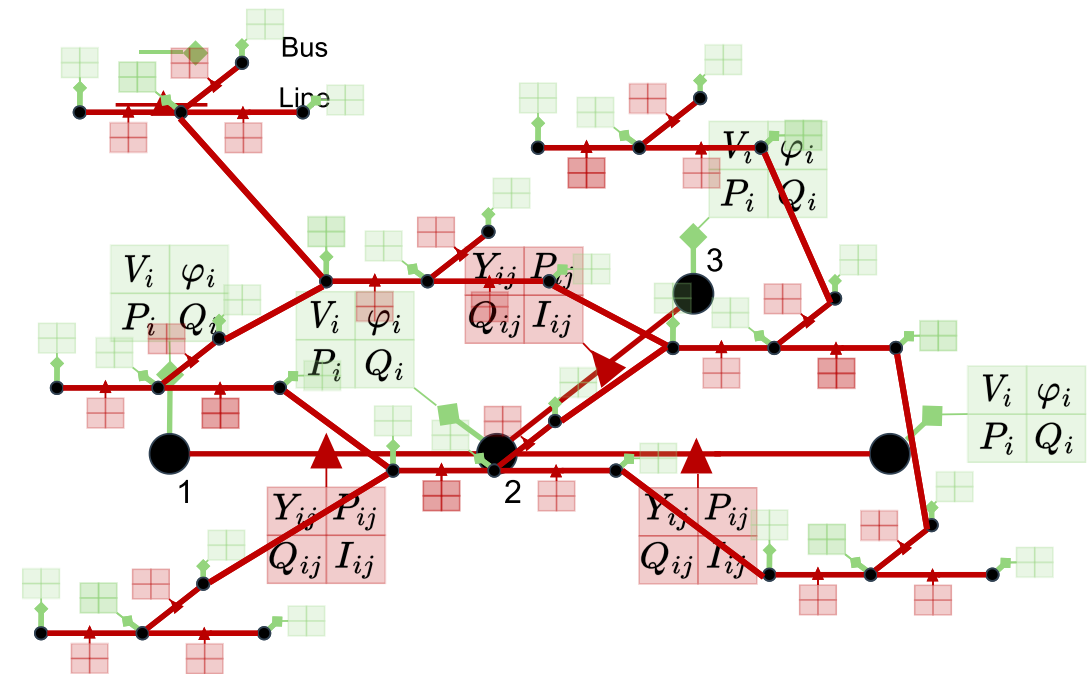
- (1-hop) neighbourhood $N_i = \{j: (i, j) \in E \cup (j, i) \in E\}$ for a node i
- Neighbourhood features $\mathbf{X}_{N_i} = \{\{x_j: j \in N_i\}\}$
- Local function, $\phi(x_i, \mathbf{X}_{N_i})$, operating over them.

Convolutional layers & message passing



$$\eta_i = \phi \left(x_i, \bigoplus_{j \in N_i} \psi(x_i, x_j) \right)$$

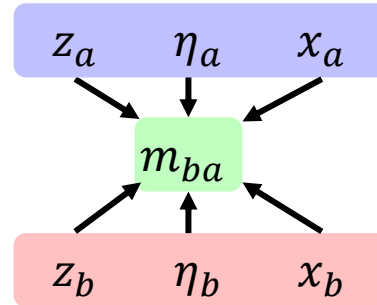
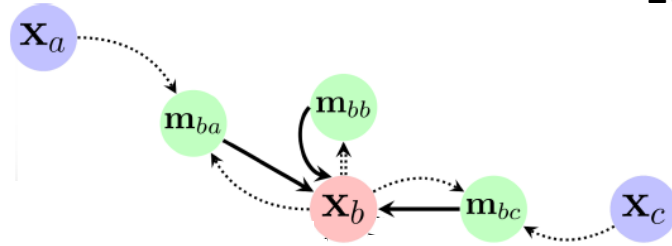
State estimation



Deep statistical solver

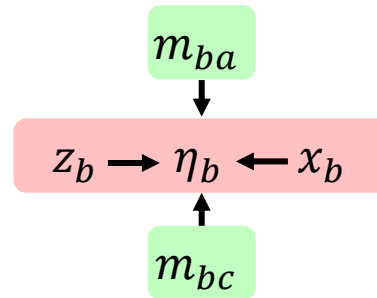
0. Initialize $x = x^0, \eta = \eta^0$

1. update edges



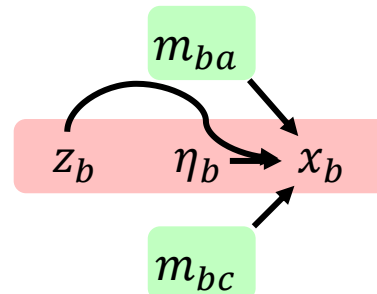
$$m_{ba} \leftarrow m_{ba} + \Delta t \times [\phi_{\theta}^{ba}(t, z_a, \eta_a, x_a) + \phi_{\theta}^{ba}(t, z_b, \eta_b, x_b)]$$

2. update vertices



$$\eta_b \leftarrow \eta_b + \Delta t \times \phi_{\theta}^b(t, z_b, \eta_b, x_b, m_{ba}, m_{bc}, m_{bb})$$

3. update label

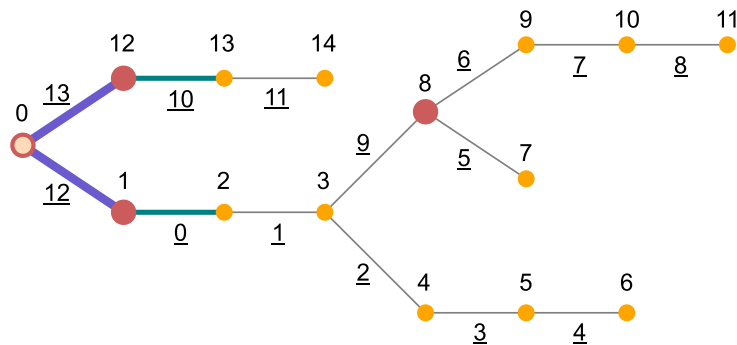


$$x_b \leftarrow x_b + \Delta t \times \phi_{\theta}^{bx}(t, z_b, \eta_b, x_b, m_{ba}, m_{bc}, m_{bb})$$

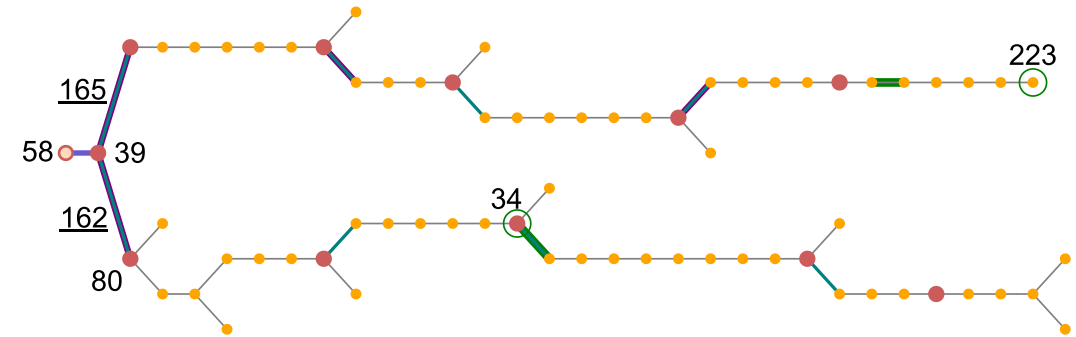
Perform $t = 1, \dots, T$

Case study: power systems

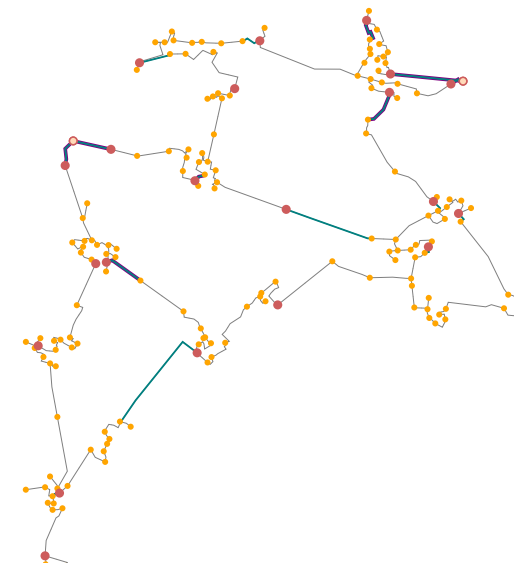
14-bus CIGRE MV grid from










70-bus Oberrhein MV sub-grid from



179-bus Oberrhein MV grid from



-  Trafo
-  Lines
-  MV/LV buses
-  HV buses
-  Power flow measurement
-  Voltage measurements
-  Focus bus

Case study settings

Data generation

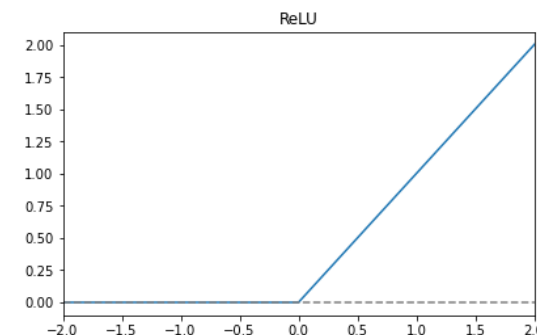
- 8640 days, with each 24 hours, +/- 15% around Gaussian on loads
- Balanced system, pandapower, AC power flow
- Measurement noise
 - 0.5% – 2% for the voltage and current measurement
 - 1% – 5% for the active and reactive power measurement
 - Pseudomeasurement were generic load profiles
- Baselines
 - Weighted least square (WLS)
 - Feedforward Neural Network (FFNN)
 - supervised DSS^2

Model & hyperparameters

- Hyper-Heterogeneous Multi GNN
- Training 80%, validation 10%, testing 10%
- Grid search on learning rate λ , layer dimensions d , and layer numbers

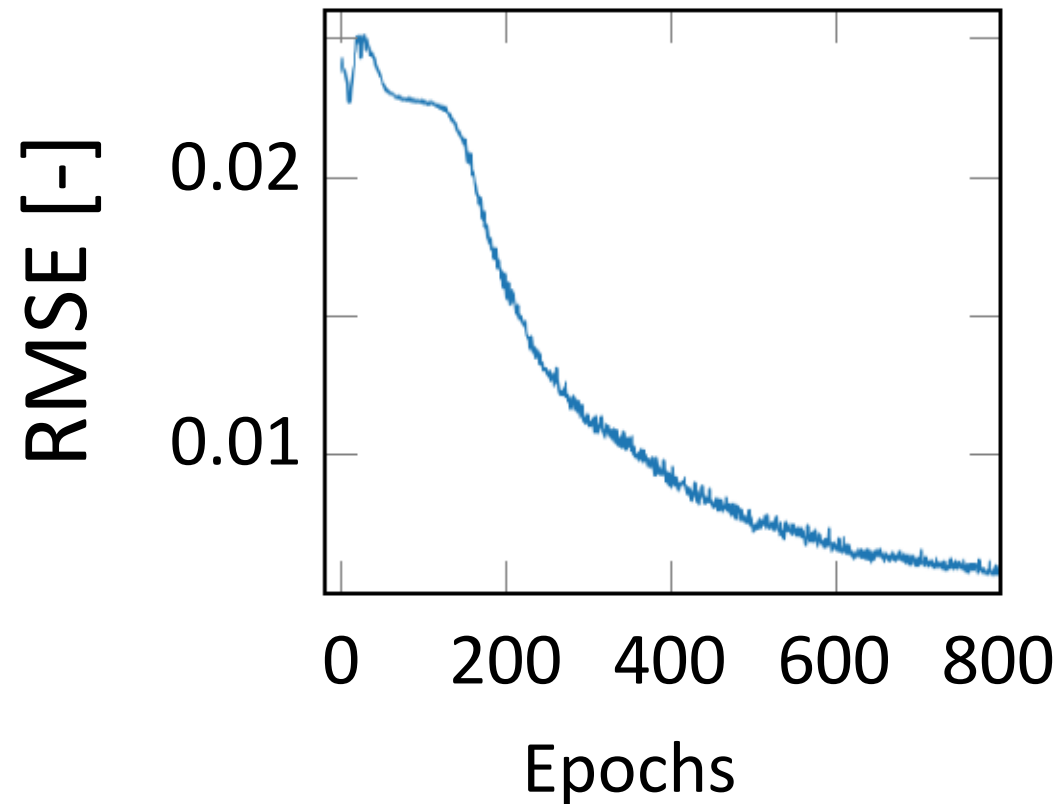
Assume stable system

$$L(z, \mathbf{x}) = \sum_{i \in m} \frac{|z_i - h_i(\mathbf{x})|^2}{R_{ii}} + \lambda [\text{ReLU}(V - 1.05) + \text{ReLU}(0.95 - V) + \text{ReLU}(\text{loading} - 100) + \text{ReLU}(\varphi - 0.25) + \text{ReLU}(-0.25 - \varphi)]$$

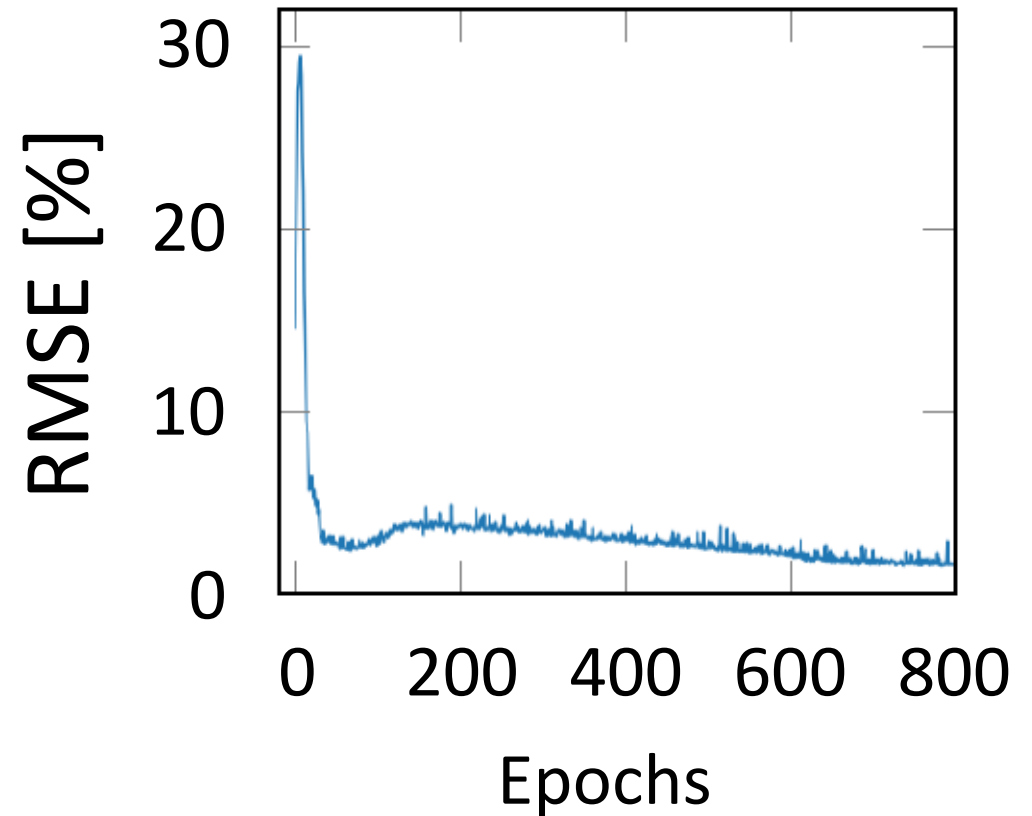


Training performance 14-bus system

Voltage levels

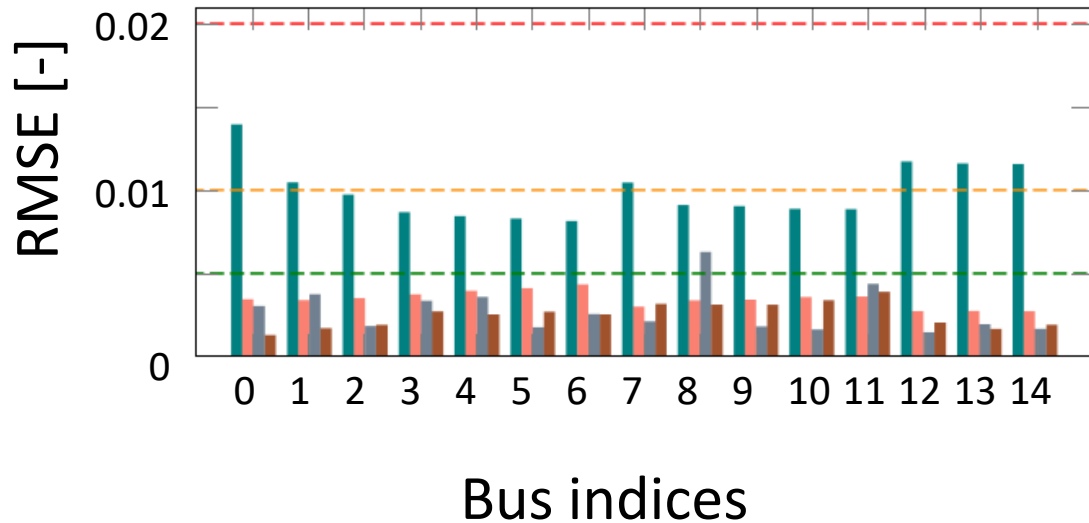


Line loadings

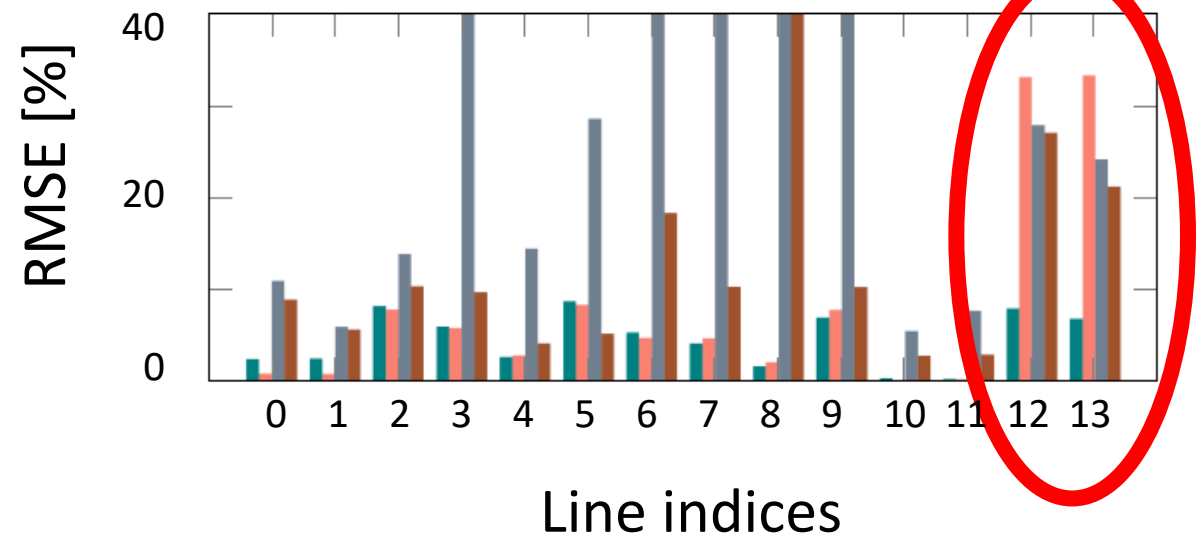


State estimation 14-bus system

Voltage levels



Line loadings



- WLS
- DSS^2
- FFNN
- DSS^2 sup.

Model inaccuracies: assumed transformer = lines!

Accuracy

Metric \ approach	14-bus system			
	WLS	ANN	sup DSS^2	DSS^2
Voltage RMSE [10^{-3}]	10	3	3	3
Line loading RMSE [%]	3	42	13	4
Trafos loading RMSE [%]	5	39	14	8

Convergence

Metric \ approach	14-bus system				70-bus Oberrhein			179-bus Oberrhein	
	WLS	ANN	sup DSS^2	DSS^2	WLS	WLS*	DSS^2	WLS**	DSS^2
Voltage RMSE [10^{-3}]	10	3	3	3	31	6	2	10	2
Line loading RMSE [%]	3	42	13	4	17	15	2	6	3
Trafos loading RMSE [%]	5	39	14	8	39	24	3	4	4
Convergence [%]	100	100	100	100	25	100	100	53	100

- WLS did not converge in some instances (25%-50%)
- DSS^2 always ‘converges’ (produces a label)

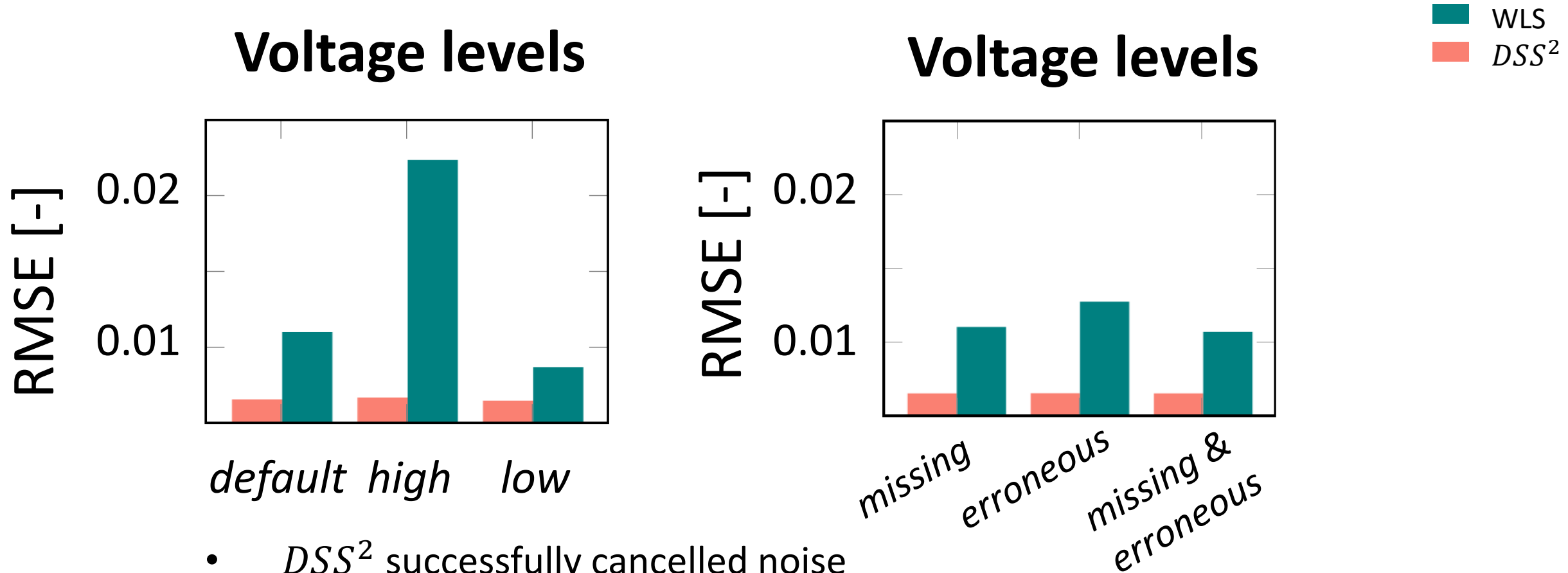
Computational ‘prediction’ time [ms]

Metric \ approach	14-bus system				70-bus Oberrhein			179-bus Oberrhein	
	WLS	ANN	sup DSS^2	DSS^2	WLS	WLS*	DSS^2	WLS**	DSS^2
Voltage RMSE [10^{-3}]	10	3	3	3	31	6	2	10	2
Line loading RMSE [%]	3	42	13	4	17	15	2	6	3
Trafos loading RMSE [%]	5	39	14	8	39	24	3	4	4
Convergence [%]	100	100	100	100	25	100	100	53	100
Computational time [ms]	86	4	5	6	123	161	26	1212	58

~10 ~2

- WLS increases significantly with system size
- DSS^2 increases moderately with system size

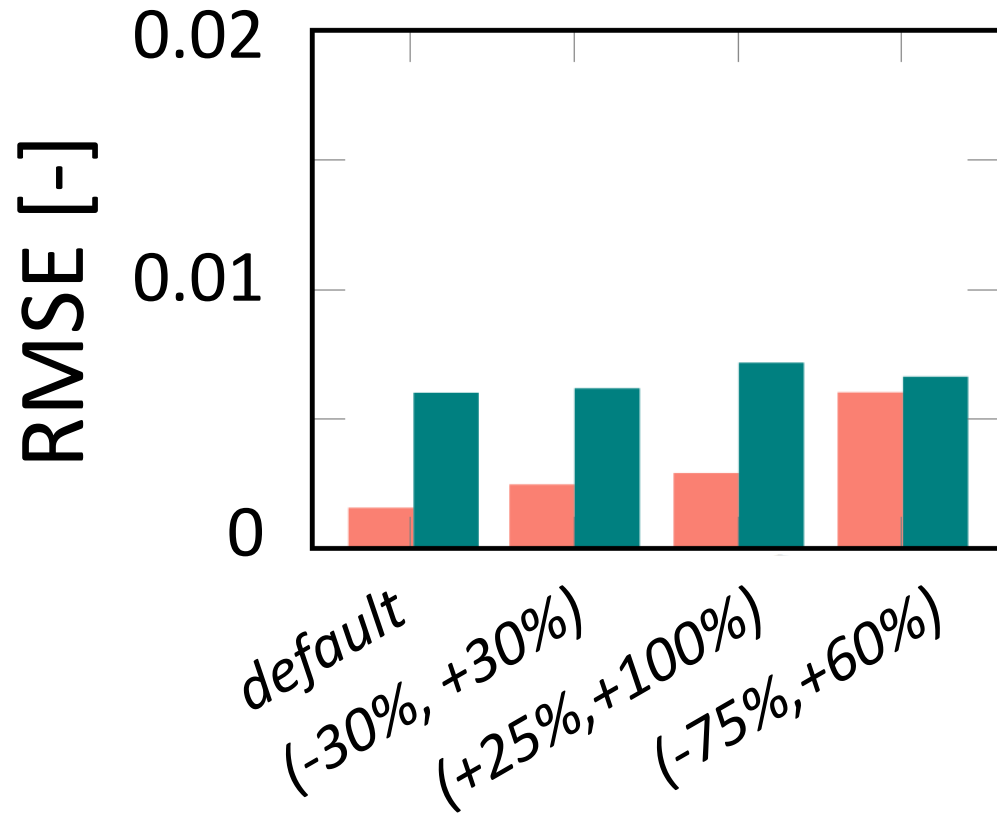
Noise and missing, erroneous data



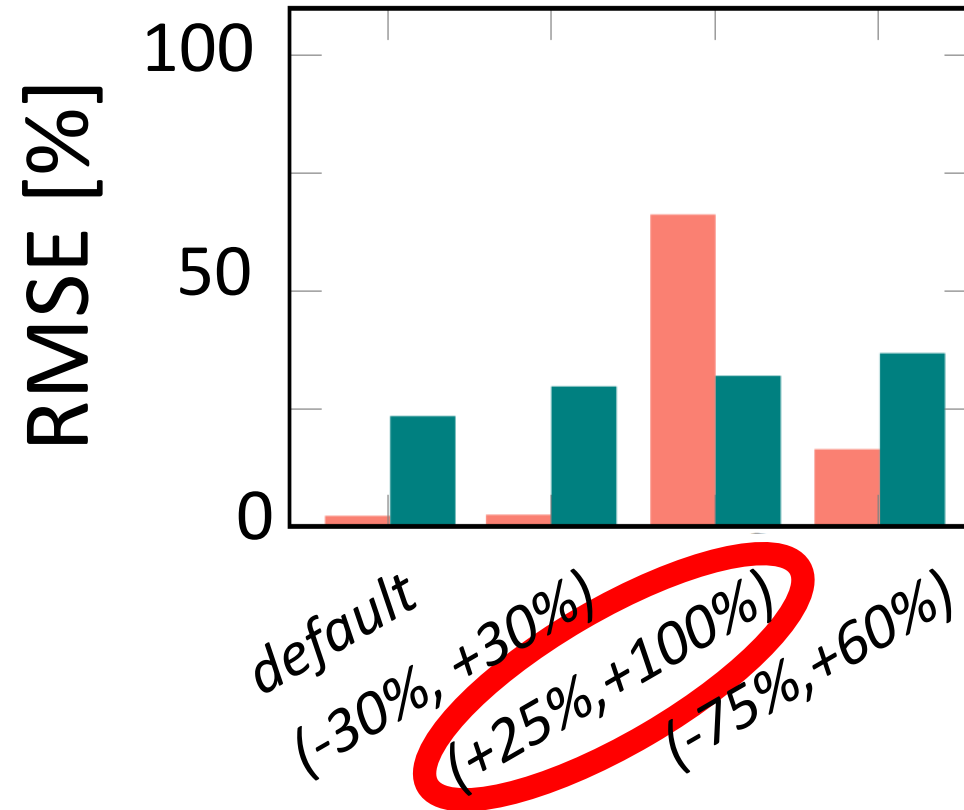
- DSS^2 successfully cancelled noise
- DSS^2 was not trained to handle such events
- GNN architecture increased the interpolation capabilities by incorporating the data symmetries w.r.t. the underlying graph

Increase in (generation, load)

Voltage levels



Line loadings



Limitation: high load levels

Drivers

- Combining interdisciplinary approaches from statistics, machine learning and mathematical optimization to a power system problem
- Learning without labels and with structural information (inducing bias, regularising with physics, etc)

Generic barriers

- Curse of dimensionality
- Performance on out-of-distribution
- Guarantees

Challenges applying GNNs to power systems

- Power systems are not always well-meshed graphs
- Enforcing power flow equations
- Addressing nonlinearity -> multiple solutions
- Graph topology changes (dynamic graphs)
- ...

Contact and references

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Benjamin Habib



Elvin Isufi



Ward van Breda



Arjen Jongepier



Reference

- B. Habib, E. Isufi, W. van Breda, A. Jongepier and J. L. Cremer, "Deep Statistical Solver for Distribution System State Estimation," in *IEEE Transactions on Power Systems*, vol. 39, no. 2, pp. 4039-4050, March 2024, doi: 10.1109/TPWRS.2023.3290358. **[open access]**
- Code: <https://github.com/TU-Delft-AI-Energy-Lab>

Related references & code

Workshop on AI for Energy Systems: https://github.com/TU-Delft-AI-Energy-Lab/Workshop_AI_for_Intelligent_Energy_Systems

Weakly supervised learning for power systems (Example code: <https://github.com/TU-Delft-AI-Energy-Lab/Deep-Statistical-Solver-for-Distribution-System-State-Estimation>**)**

- Bastien Giraud, Ali Rajaei, Jochen L. Cremer “Constraint-Driven Deep Learning for N-k Security Constrained Optimal Power Flow”, *Electric Power System Research and 2024 IEEE Power System Computation Conference*
- B. Habib, E. Isufi, W. v. Breda, A. Jongepier and Jochen L. Cremer, “Deep Statistical Solver for Distribution System State Estimation, ” *IEEE Transactions on Power Systems, 2023, doi: 10.1109/TPWRS.2023.3290358.*

Cost-sensitive learning

- Dariush Wahdany, Carlo Schmitt, Jochen L. Cremer, “More than Accuracy: End-To-End Wind Power Forecasting that Optimises the Energy System”, *Electric Power System Research, 2023*
- A. Bugaje, J. L. Cremer, M. Sun, G. Strbac, “Selecting DT Models for Security Assessment using ROC- and Cost-Curves”, *Energy and AI, 2021: 100110.*
- J. L. Cremer, G. Strbac, “A Machine-learning based Probabilistic Perspective on Dynamic Security Assessment” *International Journal of Electrical Power & Energy System, 2020*

Interpretable models (Example code: <https://github.com/JochenC/From-optimization-based-machine-learning-to-interpretable-security-rules-for-operation>**)**

- J. L. Cremer, I. Konstantelos, G. Strbac, “From Optimization-based Machine Learning to Interpretable Security Rules for Operation”, *IEEE Transactions on Power Systems, 2019*
- J. L. Cremer, I. Konstantelos, S. H. Tindemans, G. Strbac, “Data-driven Power System Operation: Exploring the Balance between Cost and Risk”, *IEEE Transactions on Power Systems, 2018*

Sampling with optimisation-based constraints (Example code: <https://github.com/TU-Delft-AI-Energy-Lab/Split-based-sampling>**)**

- Al-Amin Bugaje, Jochen L. Cremer, Goran Strbac “Generating Quality Datasets for Real-Time Security Assessment: Balancing Historically Relevant and Rare Feasible Operating Condition” *International Journal of Electrical Power & Energy Systems, 2023*

Thank you